# An online smart, interactive, collaborative, multilingual database of mathematical theorems and proofs

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This talk is available online at computo.fismat.umich.mx/~valero

Work in progress



## First proofs

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#### **Problem**

Understanding mathematical proofs is very hard for someone who is not familiar with them; writing their own proofs is even harder!

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#### ... but impractical!

But in a class of 20 or more students, the teacher may not have enough time to devote to each student to help them to understand and write proofs.

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## The website

#### A more ambitious project

We want to add much more to this website than just interactive practice with proofs, so now let's look at the big picture

## The big picture



Prooftopia is an ongoing ambitious online project, involving:

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- customized online courses based on theorems and proofs

## Final words

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## Thank you!